

- c. Three boys b_1, b_2, b_3 and four girls g_1, g_2, g_3, g_4 are such that
 b_1 is a cousin of g_1, g_2 and g_4
 b_2 is a cousin of g_2 and g_4
 b_3 is a cousin of g_2 and g_3 .
 If a boy must marry a cousin girl, find possible sets of such couples. (07 Marks)

PART – B

- 5 a. Find the number of ways of giving 10 identical gift boxes to six persons A, B, C, D, E, F in such a way that the total number of boxes given to A and B together does not exceed 4. (06 Marks)
- b. Define Catalan numbers. In how many ways can one travel in the xy plane from $(0, 0)$ to $(3, 3)$ using the moves R: $(x + 1, y)$ and U: $(x, y + 1)$ if the path taken may touch but never rise above the line $y = x$? Draw two such paths in the xy plane. (07 Marks)
- c. Determine the coefficient of
 i) xyz^2 in the expansion of $(2x - y - z)^4$
 ii) $a^3b^3c^2d^5$ in the expansion of $(a + 2b - 3c + 2d + 5)^{16}$. (07 Marks)
- 6 a. How many integers between 1 and 300 (inclusive) are
 i) divisible by 5, 6, 8?
 ii) divisible by none of 5, 6, 8? (07 Marks)
- b. In how many ways can the integers 1, 2, 3, ..., 10 be arranged in a line so that no even integer is in its natural place? (06 Marks)
- c. Find the rook polynomial for the following board (Fig.Q.6(c)). (07 Marks)



Fig.Q.6(c)

- 7 a. Find the coefficient of x^{18} in the following products:
 i) $(x + x^2 + x^3 + x^4 + x^5)(x^2 + x^3 + x^4 + x^5 + \dots)^5$
 ii) $(x + x^3 + x^5 + x^7 + x^9)(x^3 + 2x^4 + 3x^5 + \dots)^3$. (07 Marks)
- b. Using the generating function find the number of i) non negative and ii) positive integer solutions of the equation $x_1 + x_2 + x_3 + x_4 = 25$. (06 Marks)
- c. Find all the partitions of x^7 . (07 Marks)
- 8 a. Solve the Fibonacci relation
 $F_{n+2} = F_{n+1} + F_n$ for $n \geq 0$ given $F_0 = 0, F_1 = 1$. (07 Marks)
- b. Solve the recurrence relation
 $a_{n-2} + a_{n-1} + a_n = 5n$. (07 Marks)
- c. Find a generating function for the recurrence relation
 $a_r + 5a_{r-1} + 6a_{r-2} = 3r^2, r \geq 2$. (06 Marks)
