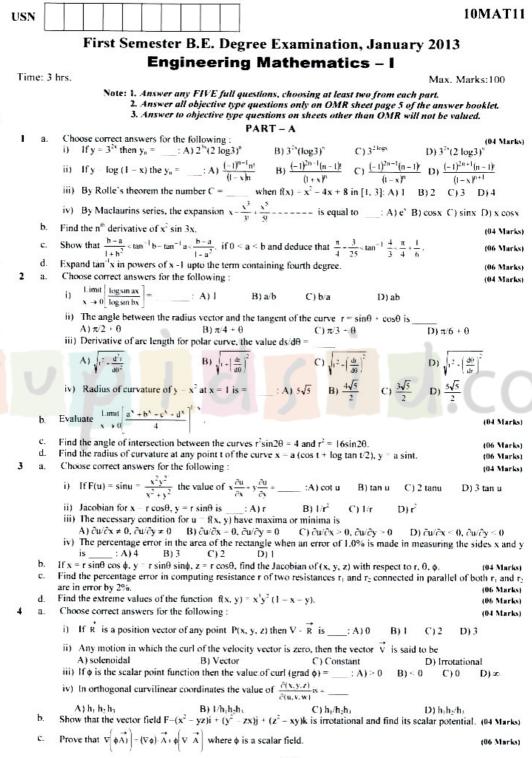
USN	N	10M/	AT11						
00000	L	First Semester B.E. Degree Examination, January 2013							
	Engineering Mathematics – I								
Tin	Time: 3 hrs. Max. Marks:10								
		Note: 1. Answer any FIVE full questions, choosing at least two from each part.							
		2. Answer all objective type questions only in OMR sheet page 5 of the answer booklet.							
		3. Answer to objective type questions on sheets other than OMR will not be valued.							
1	a.	Choose the correct answers for the following : $\frac{PART - A}{PART - A}$							
10	a.	i) The Leibnitz theorem is the formula to find the n <sup>th</sup> derivative of							
		A) trigonometric function B) exponential function C) product of two algebraic functions D)product of two functions							
		ii) The n <sup>th</sup> derivative of $5^x$ is : A) log 5, $5^x$ B) $(\log 5)^n 5^x$ C) $e^{(\log 5)x}$ D) $(\log 5)^2 e^{(\log 5)x}$							
		iii) The value of 'c' of the Cauchy mean value theorem for $f(x) = c'$ , $g(x) = c''$ in (3, 7) is : A) 5 B) 3 C) 0 I iv) The generalized series of Maclaurin's series expansion is	D) 4						
		이렇게 가장 이렇게 잘 알았다. 집에 집에 이렇게 이렇게 잘 많이 많이 많이 많이 많이 많이 많이 많이 많이 봐. 이렇게 이렇게 들었다. 말 나는 것 같은 것 같	Marks)						
	b.	Verify Rolle's theorem for the function $f(x) = x^2 (1-x)^2$ in $0 \le x \le 1$ and also find the value of c. (04)	Marks)						
	c.	If $\sin^{-1} y = 2\log(x+1)$ , prove that $(x+1)^2 y_{n+2} + (2n+1)(x+1)y_{n+1} + (n^2+4)y_n = 0$ . (06)	Marks)						
	d.		Marks)						
2	a,	Choose the correct answers for the following :							
100 - 8		i) The curve $r = \frac{a}{1 + \cos \theta}$ intersect orthogonally with the following curve : A) $r = \frac{b}{1 - \cos \theta}$ B) $r = \frac{c}{1 + \sin \theta}$ C) $r = \frac{b}{1 - \sin \theta}$ D) $r = \frac{b}{1 - \sin \theta}$	d						
		i) If $\phi$ be the angle between the tangent and radius vector at any point on the curve $r = f(\theta)$ , then sin $\phi$ equals to	cost						
		A) dr B) $d\theta$ C) $d\theta$ D) $dr$							
		$\frac{ds}{ds}$ $\frac{ds}{dr}$ $\frac{dr}{d\theta}$							
		A) $\frac{dr}{ds}$ B) $r \frac{d\theta}{ds}$ C) $r \frac{d\theta}{dr}$ D) $r \frac{dr}{d\theta}$ iii) L Hospital's Rule can be applied to the limits of the form:A) $0/0$ B) $0 \times \infty$ C) $\infty - \infty$ D) $\infty^0$ iv) Lt $(a^{1/x} - 1)x$ is of the following form:A) $0 \times \infty$ B) $\infty - \infty$ C) $\infty^0$ D) $0^x$							
		iv) Lt $(a^{1,x} - 1)_X$ is of the following form $(a^{1,x} - 1)_X = (a^{1,x} - 1)_$	Marks)						
	b.	Evaluate $\lim_{x \to 0^{-2}} (\tan x)^{\max}$ (04	Marks)						
	c.		Marks)						
	d.		Marks)						
3	a.	Choose the correct answers for the following :							
- 59		i) If $f(x,y) = \frac{1}{x^3} + \frac{1}{y^4} + \frac{1}{x^2 + y^3}$ , then $x \frac{\partial f}{\partial x} + y \frac{\partial f}{\partial y}$ is : A) 0 B) 9 C) 1 D) -3f							
		ii) If $\mathbf{x} = \rho \cos \theta$ , $\mathbf{y} = \rho \sin \theta$ , $\mathbf{z} = \mathbf{z}$ then $\frac{\hat{c}(\mathbf{x}, \mathbf{y}, \mathbf{z})}{\hat{c}(\rho, \theta, \mathbf{z})}$ : A) $\rho$ B) 1 C) 0 D) $\theta$							
		iii) If an error of 1% is made in measuring its base and height, the percentage error in the area of a triangle is							
		A) 0.2% B) 0.02% C) 1% D) 2%							
		iv) One of the necessary and sufficient condition for a function to have a maximum value is A) AC - B <sup>2</sup> > 0, A < 0 B) AC - B <sup>2</sup> = 0, A = 0 C) AC - B <sup>2</sup> < 0, A > 0 D) AC - B <sup>2</sup> > 0, A > 0 (04)	Market						
			Marks)						
	b.	If $V = e^{i\theta} \cos(a \log r)$ , prove that $\frac{\partial^2 v}{\partial r^2} + \frac{1}{r} \frac{\partial v}{\partial r} + \frac{1}{r^2} \frac{\partial^2 v}{\partial \theta^2} = 0$ . (06)	Marks)						
	c.	Examine the function $f'(x, y) = 1 + \sin(x^2 + y^2)$ for extremum values. (05)	Marks)						
	d.	In calculating the volume of right circular cone, errors of 2% and 1% are made in height and radius of the base respectively. F							
10			Marks)						
4	a.	Choose the correct answers for the following : $\vec{E} = \vec{E}$							
		i) If $\vec{F} = \nabla \phi$ , then the curl $\vec{F}$ : A) solenoidal B) irrotational C) rotational D) none of these ii) If $V = x^2 + y^2 + 3$ then grad V is: A) $2xi + 2yj$ B) $2x + 2y$ C) $2xi + 2yj + k$ D) $xi + yj$							
		ii) If $V = x^2 + y^2 + 3$ then grad V is : A) $2xi + 2yj$ B) $2x + 2y$ C) $2xi + 2yj + k$ D) $xi + yj$ iii) The value of 'a' of the vector $\vec{F} = (x + 3y)i + (x - 2z)j + (x + az)k$ , which is solenoidal : A) $-2$ B) $-1$ C) $0$ D)	17						
			Marks)						
6	b.		Marks)						
0	c.		Marks)						
	d.		Marks)						
<u>PART – B</u>									
5 a. Choose the correct answers for the following : $\frac{\pi^2}{2}$									
		i) The value of $\int_{\cos x \sin^{20} x  dx}^{\pi/2} \sin^{20} x  dx$ is A) 1/99 B) 1/100 C) $\pi/100$ D) 99/100							

		(i) The sum $-3(-2) + (2) = -3(-2) - 2(-3) + (-3) $	10MAT11
		<ul> <li>ii) The curve y<sup>2</sup>(a<sup>2</sup> + x<sup>2</sup>) = x<sup>2</sup>(a<sup>2</sup> - x<sup>2</sup>) is</li> <li>A) symmetric about the x-axis</li> <li>B) symmetric about the x &amp; y axis</li> <li>C) symmetric about the y-axis</li> <li>D) nor</li> <li>iii) The length of the arc y = f(x) from x = a to x = b is</li> </ul>	ne of these
		A) $\int_{a}^{b} \sqrt{1 + \left(\frac{dy}{dx}\right)^2} dx$ B) $\int_{a}^{b} \sqrt{1 + \left(\frac{dx}{dy}\right)^2} dx$ C) $\int_{a}^{b} \sqrt{1 + \left(\frac{dx}{dy}\right)^2} + \left(\frac{dy}{dx}\right)^2} dx$ D) none of these	
		iv) The value of $\int_{0}^{\pi} \sin^4 x  dx$ is equal to : A) $3\pi/8$ B) $3/8$ C) $\pi/16$ D) $\pi/4$	(04 Marks)
	b.	Obtain the reduction formula for $\int \sin^n x  dx$ .	(04 Marks)
	c.	Evaluate $\int_{-\infty}^{\infty} x \sqrt{ax - x^2} dx$	(06 Marks)
	d.	Find the area of an arch of the cycloid $x = a(\theta - \sin \theta)$ , $y = a(1 - \cos \theta)$ .	(06 Marks)
5	a.	Choose the correct answers for the following :	
		i) The order and degree of the differential equation $\left[1 + \left(\frac{dy}{dx}\right)^2\right]^2 = c \frac{d^2y}{dx^2}$ respectively is	
		A) one, two B) one, one C) two, one D) three, two	
		ii) The differential equation $\left[1 + e^{x/x}\right]dx + e^{x/x}\left[1 - \frac{x}{y}\right]dy = 0$ is	
		A) homogeneous and linear B) homogeneous and exact C) non-homogeneous and exact D) none of th	
		iii) The solution of the differential equation $\frac{dy}{dx} = e^{x+x}$ : A) $e^x + e^y = c$ B) $e^x + e^y = c$ C) $e^x - e^{-y} = c$ D) $e^{x^2}$	) = c
		iv) Replacing $dy/dx$ by $-dx/dy$ in the differential equation of $(x, y, dy/dx) = 0$ , we get the differential equation of A) polar trajectory B) orthogonal trajectory C) trajectory D) none of these	(04 Marks)
	b.	Solve $\frac{dy}{dx} = \frac{2x - y + 1}{x + 2x - 3}$ .	(06 Marks)
	с,		The Party State
		Solve $dr + (2r \cot \theta + \sin 2\theta)d\theta = 0$ .	(06 Marks)
	d.	Find the orthogonal trajectory of the family of coaxial circles $\frac{x^2}{a^2} + \frac{y^2}{b^2 + \lambda} = 1$ .	(04 Marks)
	a,	Choose the correct answers for the following :	
		i) The normal form of the matrix are A) $[I_3, 0]$ B) $\begin{bmatrix} I^2 \\ 0 \end{bmatrix}$ C) $\begin{bmatrix} I_3, 0 \\ 0 & 0 \end{bmatrix}$ D) all of ii) The solution of the simultaneous equations $x + y = 3$ , $x - y = 3$ is	these
		ii) The solution of the simultaneous equations $x + y = 3$ , $x - y = 3$ is A) only trivial B) only unique C) unique and trivial D) none of these	
		iii) In Gauss Jordan method, the coefficient matrix reduces to matrix	
		A) diagonal B) unit matrix C) triangular matrix D) none of these iv) If r is the rank of the matrix [A] of order $m \times n$ then r is : A) $r \le m$ B) $r \le n$ C) $r \ge n$ D) $r \ge m$	(04 Marks)
		[0 2 3 4 ]	
	b.	Find the rank of the following matrix by elementary transform: $A = \begin{bmatrix} 2 & 3 & 5 & 4 \\ 4 & 8 & 13 & 12 \end{bmatrix}$	(04 Marks)
	C_	Find for what value of k the system of equations $x + y + z = 1$ , $x + 2y + 4z = k$ , $x + 4y + 6z = k^2$ , posses a solu	
	d.	completely in each case. Solve the following system of equations by Gauss elimination method: $x + y + z = 9$ ; $x - 2y + 3z = 8$ ; $2x + y - z = 3$	(06 Marks) (06 Marks)
	a.	Choose the correct answers for the following :	
		<ul> <li>i) If the determinant of the coefficient matrix is zero, then there exist</li> <li>A) trivial solution</li> <li>B) non-trivial solution</li> <li>C) unique solution</li> <li>D) no solution</li> </ul>	
		(2) ICD is the model model of the order and model at the factor of the factor of the	
		A) $P_{-}^{(1)}$ B) P C) diagonal matrix D) none of these iii) The quadratic form for the matrix $\begin{bmatrix} a & b \end{bmatrix}$ is : A) $ax^2 + 2hxy + by^2$ B) $ax^2 + by^2$ C) $ax^2 + 2bxy + 2by^2$ D) non	6.0
		(i) If P is the modal matrix of an orthogonal matrix, then its inverse matrix is equal to (A) $P^{-1}$ (B) $P$ (C) diagonal matrix (D) none of these (iii) The quadratic form for the matrix $A = \begin{bmatrix} a & h \\ h & b \end{bmatrix}$ (is : A) $ax^2 + 2hxy + by^2$ (B) $ax^2 + 2bxy + 2by^2$ (D) $ax^2 + 2bxy + 2by^2$ (D) non (iii) The nature of the quadratic function of the matrix having the eigen values [0, 2, 4] is	e of these
		A) positive definite B) positive semi-definite C) negative definite D) negative semi-definite	(04 Marks)
	b.	Reduce the matrix $A = \begin{bmatrix} -1 & 3 \\ -2 & 4 \end{bmatrix}$ to the diagonal form and hence find $A^4$ .	(06 Marks)
	c	Find all the eigen values of the matrix $A = \begin{bmatrix} 8 & -6 & 2 \\ -6 & 7 & -4 \\ 2 & -4 & 3 \end{bmatrix}.$	(04 Marks)
	d.	Reduce the quadratic form $3x^2 + 3y^2 + 3z^2 + 2xy - 2yz + 2zx$ into canonical form.	(06 Marks)
		*****	



Inportant Note : 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages. 2. Any revealing of identification, appeal to evaluator and /or equations written eg. 42+8 – 50, will be treated as malpractice.

## 10MAT11

	d.	If $\vec{F}(u,v,w)$ be the vector point function given interms of orthogonal curvilinear coordinates as $F = F_1 e_1 + F_2 e_2 + F_3 e_3$ ,
		find curl F. (06 Marks)
		PART – B
5	a.	Choose correct answers for the following -
		i) If $I(\alpha) = \int_{0}^{1} \left[ \frac{x^{\alpha} - 1}{\log x} \right] dx$ then $\frac{dI(\alpha)}{d\alpha} = $ : A) 4/(1+\alpha) B) 3/(1+\alpha) C) 2/(1+\alpha) D) 1/(1+\alpha)
		ii) The value of $\int_{0}^{\pi} \sin^4 x  dx$ is =: A) $3\pi/8$ B) $3\pi/16$ C) $3\pi^2/8$ D) Zero
		iii) A curve $r = a (1 + cos0)$ has the length on x-axis (the initial finity) (A) $\pm a = (1 + cos0)$ has the length on x-axis (the initial finity) (A) $\pm a = (1 + cos0)$ and $y = (1 + cos0)$ has the length on x-axis (the initial finity) (A) $\pm a = (1 + cos0)$ has the length on x-axis (the initial finity) (A) $\pm a = (1 + cos0)$ has the length on x-axis (the initial finity) (A) $\pm a = (1 + cos0)$ has the length on x-axis (the initial finity) (A) $\pm a = (1 + cos0)$ has the length on x-axis (the initial finity) (A) $\pm a = (1 + cos0)$ has the length on x-axis (the initial finity) (A) $\pm a = (1 + cos0)$ $\pm (1 + cos0$
	b.	Differentiate under the integral sign and hence evaluate the integration $\int_{0}^{\infty} \frac{\tan^{-1}(ax)}{x(1+x^2)} dx$ (04 Marks)
	c.	Evaluate $\int_{0}^{2\pi} x^{2} \left( \sqrt{2\pi x - x^{2}} \right) dx = (06 \text{ Marks})$
	d.	Trace the curve $r = a (1 + \cos\theta)$ and hence find the total length. (06 Marks)
6	a.	Choose correct answers for the following : (04 Marks) i) The solution of the differential equation $dy/dx = e^{x^2y}$ is
		A) $e^{x}/e^{x} = c$ B) $e^{x}/e^{x} = c$ C) $e^{x} + e^{x} = c$ D) $e^{x}/e^{x} = c$
		ii) If $M(x, y)dx + N(x, y) dy = 0$ is said to be exact then the condition is
		A) $\partial M/\partial y \neq \partial N/\partial x$ B) $\partial M/\partial y = \partial N/\partial x$ C) $\partial M/\partial y \geq \partial N/\partial x$ D) $M = N$ iii) The integrating factor for $(x + 2y^3) dy/dx = y$ is $I.F = $ : A) $\log y$ B) $e^{y}$ C) $I/y$ D) $y + 1$
		and the second sec
		(iv) For $r = f(\theta)$ , the replacement of dride to find the orthogonal narcedly is (A) $-r\frac{dr}{d\theta}$ (B) $-r^2\frac{dr}{d\theta}$ (C) $-r^2\frac{d\theta}{dr}$ (D) $-r\frac{d\theta}{dr}$
	b.	Solve $(4x + 6y + 5) dy = (3y + 2x + 4) dx$ , (64 Marks)
	с.	(b) that so
	d.	Solve $dy/dx + x \sin 2y = x \cos y$ . Find the orthogonal trajectory of the system of confocal conics $x^2/(a^2+\lambda) + y^2/(b^2+\lambda) = 1$ where $\lambda$ is the parameter. (06 Marks)
7	a.	Choose correct answers for the following : $(04 \text{ Marks})$
		i) The system of linear equations is said to be consistent then the relation between $R(A)$ and $R(A:B)$ in $AX = B$ is $(A) = R(A) > R(A) > R(A:B)$ B) $R(A) < R(A:B)$ C) $R(A) \neq R(A:B)$ D) $R(A) = R(A:B)$
		is: A) $R(A) \ge R(A;B)$ B) $R(A) \le R(A;B)$ C) $R(A) \ne R(A;B)$ D) $R(A) = R(A;B)$ [1 3 -2]
		is (A) $K(A) > K(A,B)$ (A) $K(A,B)$
		iii) A square matrix is said to be symmetric matrix is (A) $a_{ij} = a_{ij}$ (B) $a_{ij} = a_{ij}$ (C) $a_{ij} = a_{ij}$ (C) $a_{ij} = a_{ij}$
		iv) In Gauss elimination method the system of equations is transformed into an D) Linner triangular matrix
		A) Row matrix D/ Column Joan A
	h	Find the rank of the matrix $A = \begin{bmatrix} 1 & 2 & -2 & 3 \\ 2 & 5 & -4 & 6 \\ -1 & -3 & 2 & -2 \\ 2 & 4 & -1 & 6 \end{bmatrix}$ . (04 Marks)
	b,	-1 -3 -2 -2
		Investigate the value of $\lambda$ and $\mu$ , so that the equations $2x + 3y + 5z = 9$ , $7x + 3y - 2z = 8$ , $2x + 3y + \lambda z = \mu$ have
	С,	is Uninvested attion: ii) No solution: iii) An infinite number of solutions.
	d.	Solve the system of equations by Gauss Jordon method: $2x+5y+7z = 52$ , $2x+y+z = 0$ , $x+y+z = 5$ .
8	a.	Choose correct answers for the following:
		B) Linearly dependent B) Linearly dependent C) Consistent D) meetistent
		$\cdots$ A is called extrement if A) A = A' B) A(A) = 1 (1) A(A = 1) (2) A(B) = 1
		ii) A matrix A is called orthogonal if $A = A = D$ with $A = A = D$ with $A = D$ (A) if $A = A = D$ (A) if $A $
		iv) A homogeneous polynomial of second degree in n variables x <sub>1</sub> , x <sub>2</sub> is called a
		A) Canonical form B) Linear form C) Exponential form D) Quadratic form Show that the transformation $y_1 = 2x_1 + x_2 + x_1$ , $y_2 = x_1 + x_2 + 2x_3$ , $y_3 = x_1 - 2x_3$ is regular, write down the inverse
	b.	transformation
	c.	Find the Eigen values and the corresponding Eigen vectors of the matrix $A = \begin{bmatrix} 1 & 1 & 3 \\ 1 & 5 & 1 \\ 3 & 1 & 1 \end{bmatrix}$ (06 Marks)
	d.	transformation.
		2 of 2