

mportant Note: 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages. 2. Any revealing of identification, appeal to evaluator and tor equations written eg. 42+8 = 50, will be treated as malpractice.

PART-B 5 a. Choose correct answers for the following : (04 Marks) i) $\int_{-\infty}^{+\infty} dy dx$ is equal to: A) 1/2 B) -1/2 C) 1/4 D) 2/5 ii) The integral $\int_{-\infty}^{\infty} e^{-(x^2+y^2)} dx dy$ by changing to polar form becomes A) $\int_{\theta=0}^{\pi/2} \int_{\tau=0}^{\pi} e^{\tau^2} r \, dr d\theta$ B) $\int_{\theta=0}^{\pi/2} \int_{\tau=0}^{\pi} e^{-\tau^2} r \, dr d\theta$ C) $\int_{\theta=0}^{\pi/2} \int_{\tau=0}^{\pi} e^{2\tau} \, dr d\theta$ iii) $\beta(3, \frac{1}{2})$ is equal to: A) 16/11 B) 16/15 C) 15/16 D) $2\pi/3$ D) none of these iv) The integral $2 \int e^{-x^2} dx$ is : A) $\Gamma(3/2)$ B) $\Gamma(n+1)$ C) $\Gamma(-1/2)$ D) T(1/2) Evaluate by changing the order of integration $\int\limits_{a}^{a} \int\limits_{-\infty}^{2\sqrt{x}a} x^2 dy dx$, a > 0,(04 Marks) Evaluate the integral $\int\limits_{-\infty}^{+\infty} \int\limits_{-\infty}^{\sqrt{1-x^2}-\sqrt{1-x^2-y^2}} xyz\,dzdydx$. С. (06 Marks) d. Prove that $\int_{-\infty}^{\infty} x e^{-x^4} dx \times \int_{-\infty}^{\infty} x^2 e^{-x^4} dx = \frac{\pi}{16\sqrt{2}}$. (06 Marks) 6 - a -Choose correct answers for the following : (04 Marks) i) If $f = (5xy - 6x^2)i + (2y - 4x)j$ then $\int f dr$ where c is the curve $y = x^3$ from the points (1, 1) to (2, 8) is A) 35 B) -35 C) 3x + 4yD) none of these ii) In Green's theorem in the plane $\int (Mdx + Ndy) =$ _____ A) $\iint_{X} \left(\frac{\partial N}{\partial x} - \frac{\partial M}{\partial y} \right) dx dy \qquad \qquad B) \iint_{X} \left(\frac{\partial N}{\partial x} - \frac{\partial M}{\partial y} \right) dx \qquad \qquad C) \iint_{X} \left(\frac{\partial M}{\partial x} - \frac{\partial N}{\partial y} \right) dy dx \qquad \qquad D) \iint_{X} \left(\frac{\partial M}{\partial x} - \frac{\partial N}{\partial y} \right) dx dy$ iii) If $\int d\mathbf{r} = 0$ then f is called: A) rational B) irrotational C) solenoidal D) rotational iv) If all the surfaces are closed in a region containing volume V then the following theorem is applicable A) Stoke's theorem B) Green's theorem C) Gauss divergence theorem D) none of these If $f = (2x^2 - 3z)i - 2xyj - 4xk$, evaluate [curl f dv] where v is the volume of the region bounded by the planes x = 0, y = 0. z = 0 and 2x + 2y + z = 4. (04 Marks) Verify Green's theorem for $\int (3x^2 - 8y^2) dx + (4y - 6xy) dy$ where c is the triangle formed by x = 0, y = 0 and x + y = 1. (06 Marks) d., Verify the Stokes's theorem for $f = -y^{\dagger}\hat{i} + x^{\dagger}\hat{j}$ where s is the circular disc $x^{2} + y^{2} \le 1$, z = 0. (06 Marks) 7 Choose correct answers for the following : a (04 Marks) i) The Laplace transform of f(t)/t when L[f(t)] = F(s) is: A) $\int_{-\infty}^{\infty} F(s)ds$, B) $\int_{-\infty}^{\infty} F(s)ds$, C) $\int_{-\infty}^{\infty} F(s-a)ds$, D) $\int_{-\infty}^{\infty} F(s+a)ds$ ii) $L[t^3e^{2t}] =$ B) $(3!)/(s+2)^4$ ___. A) (3!)/(s-2)⁴ C) $3/(s-2)^4$ D) 3/(s-2)iv) $L\{\delta(t)\}$ is equal to : A) 0 B) -1 C) e^{as} D) L b. Evaluate 1.(sint sin 2t sin 3t). (04 Marks) A periodic function of period $2\pi/\omega$ is defined by $f(t) = \begin{cases} E \sin \omega t & \text{for } 0 \le t \le \pi/\omega \\ 0 & \text{for } \pi/\omega \le t \le 2\pi/\omega \end{cases}$. Find L{f(t)}. C. (06 Marks) d. Express $f(t) = \begin{cases} 2t & 0 < t \le \pi \\ 1 & t \ge \pi \end{cases}$ in terms of unit step function and hence find L{f(t)}. (06 Marks) Choose correct answers for the following : a. . (04 Marks) $\tilde{i}) = L^{-1}\{F(s)/s\} \text{ is equal to }; A) = \int_{-1}^{1} f(t)dt = B) = \int_{-1}^{\infty} f(t)dt = C) = \int_{-1}^{\infty} f(t-a)dt = D) = \int_{-1}^{1} f(t-a)dt = D$ ii) $L^{-1} \{ 1/(s^2 + 2s + 5) \}$ is equal to : A) $e^t \sin 2t$ B) $1/2 e^t \sin 2t$ C) $1/2 e^t \cos 2t$ D) $e^{2t} \cos 2t$ iii) f(t) * g(t) is defined by: A) $\int f(t-u)g(u)du = B$ $\int f(t)g(t)dt = C$ $\int f(t)g(t)du = D$ $\int f(u)g(u)du$ iv) $L^{-1} \{1/(s^2 + a^2)\}$ is : A) cos at B) sec at C) sin at D) (1/a) sin at b. Find $L^{-1}\{(2s-1)/(s^2+2s+17)\}$. (04 Marks) C. By employing the convolution theorem evaluation $L^4 \{s/(s^2 + a^2)^2\}$. (06 Marks) Solve the initial value problem $y'' - 3y' + 2y = 4t + e^{3t}$, y(0) = 1, y'(0) = -1 using Laplace transforms. d. (06 Marks)

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