

PART – B

- 5 a. Using Newton-Raphson method find a real root of $x + \log_{10} x = 3.375$ near 2.9, corrected to 3-decimal places. (07 Marks)
- b. Solve the following system of equations by relaxation method:
 $12x + y + z = 31$, $2x + 8y - z = 24$, $3x + 4y + 10z = 58$ (07 Marks)
- c. Find the largest eigen value and corresponding eigen vector of following matrix A by power method

$$A = \begin{bmatrix} 25 & 1 & 2 \\ 1 & 3 & 0 \\ 2 & 0 & -4 \end{bmatrix}$$

Use $X^{(0)} = [1, 0, 0]^T$ as the initial eigen vector.

(06 Marks)

- 6 a. In the given table below, the values of y are consecutive terms of series of which 23.6 is the 6th term, find the first and tenth terms of the series. (07 Marks)

x	3	4	5	6	7	8	9
y	4.8	8.4	14.5	23.6	36.2	52.8	73.9

- b. Construct an interpolating polynomial for the data given below using Newton's divided difference formula. (07 Marks)

x	2	4	5	6	8	10
f(x)	10	96	196	350	868	1746

- c. Evaluate $\int_0^1 \frac{x}{1+x^2} dx$ by Weddle's rule taking 7-ordinates and hence find $\log_e 2$. (06 Marks)

- 7 a. Solve the wave equation $u_{tt} = 4u_{xx}$ subject to $u(0, t) = 0$; $u(4, t) = 0$; $u_t(x, 0) = 0$; $u(x, 0) = x(4 - x)$ by taking $h = 1$, $k = 0.5$ upto four steps. (07 Marks)

- b. Solve numerically the equation $\frac{\partial u}{\partial t} = \frac{\partial^2 u}{\partial x^2}$ subject to the conditions $u(0, t) = 0 = u(1, t)$, $t \geq 0$ and $u(x, 0) = \sin \pi x$, $0 \leq x \leq 1$. Carryout computations for two levels taking $h = \frac{1}{3}$ and $k = \frac{1}{36}$. (07 Marks)

- c. Solve the elliptic equation $u_{xx} + u_{yy} = 0$ for the following square mesh with boundary values as shown in Fig.Q7(c). (06 Marks)

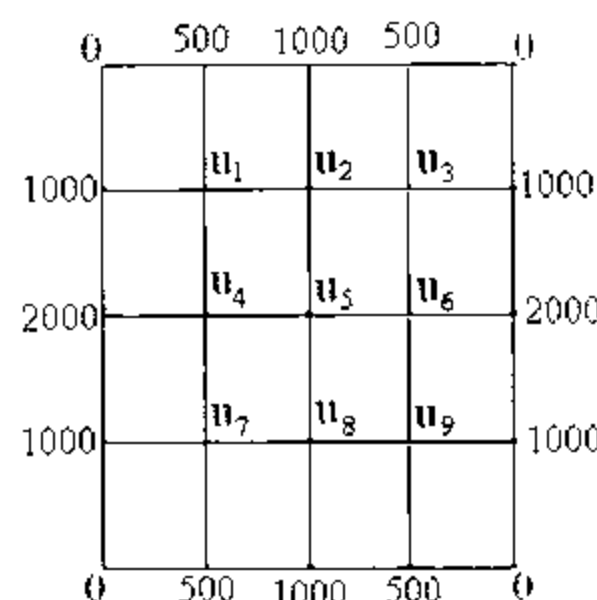


Fig.Q7(c)

- 8 a. Find the z-transform of: i) $\sin h n \theta$; ii) $\cosh h n \theta$. (07 Marks)

- b. Obtain the inverse z-transform of $\frac{8z^2}{(2z-1)(4z-1)}$. (07 Marks)

- c. Solve the following difference equation using z-transforms:
 $y_{n+2} + 2y_{n+1} + y_n = n$ with $y_0 = y_1 = 0$ (06 Marks)
